**Philadelphia University Faculty of Science** 

**Department Mathematics** Academic year 2023/2024

**Course Syllabus** 

### **Course Information**

| Course#  | Course title |  |        | Prere | equisite |
|--|--------------|--|--------|-------|----------|
| 0250251  | Graph Theory |  |        | 025   | 0241     |
| Course type Cl                                 |              |  | Class  | time  | Room     |
| □ University Requirement □ Faculty Requirement |              |  | Sat-I  | Mon   | 6606     |
| 🛛 Major Requ                                   |              |  |        | 13:30 |          |
| Compulsory                                     |              |  | Sun-   | Wed   | 21005    |
| 1  |              |  | 9:45-2 | 10:35 |          |

### **Instructor Information**

| Name                | Office<br>No. | Phone<br>No. | Office Hours            | E-mail                       |
|---------------------|---------------|--------------|-------------------------|------------------------------|
| Dr. Hani<br>Kawariq | 2824          | 2264         | S/T/M/W 11:15-<br>12:15 | hkawariq@philadelphia.edu.jo |

### **Course Delivery Method**

| Course Delivery Method        |                        |     |          |  |  |
|-------------------------------|------------------------|-----|----------|--|--|
| □ Physical □ Online ⊠ Blended |                        |     |          |  |  |
| Learning Model                |                        |     |          |  |  |
| Percentage                    | Percentage Synchronous |     | Physical |  |  |
| 0%                            |                        | 33% | 67%      |  |  |

#### **Course Description**

This course is an introduction to Graph Theory and its applications, covering topics in Graph isomorphism, Trees and its applications, Bipartite Graphs and Matching, Euler and Hamiltonian Graphs, Graph Coloring, Planar Graphs, Metrical Representations, Digraphs and Networks, with numerous graph algorithms throughout.

**Approval date:** PHILADELPHIA Issue: UNIVERSITY

Credit hours 3

THE WAY TO THE FUTURE

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**Bachelor** 

| Number    | Learning Outcomes  | Corresponding<br>Program<br>Outcomes |
|-----------|--|--------------------------------------|
|           | Knowledge  |                                      |
| K1        | Analyze the regularity of some graph. Determine whether or not a<br>sequence is graphical. Determine the Isomorphism between two<br>graphs. Produces a spanning tree of a graph. Produce a minimal<br>spanning tree a graph. The concept of the isomorphism a<br>weighted graph G. | Кр1                                  |
| K2        | Understand the concepts of Walk, Euler Walks, Cycles, Hamilton<br>Cycles. Find the distance between the vertices. Find the shortest<br>closed walk. Find the adjacency, and incidence matrices. Find the<br>distance matrix.   | Кр2                                  |
| К3        | Coloring bipartite graphs. Determine when the graph is planar.<br>Determine the Chromatic number. Understand the Regions of a<br>plane graph. Know the Maps and the dual graphs.   | Кр2                                  |
|           | Skills   |                                      |
| <b>S1</b> | Understand mathematical definitions and demonstrate it in different graphs and writing algorithms.   | Sp1                                  |
|           | Competencies   |                                      |
| C1        | Express thoughts in good logical writing (Examples, Proofs,etc)  | Cp1                                  |

# Learning Resources

| Course textbook       | Amin Witno, Discrete Structures in five chapters.  |  |  |
|-----------------------|--|--|--|
| Supporting References | <ol> <li>Lecture Notes based on Amin Witno Book.</li> <li>A Friendly Introduction to Graph Theory, by <u>Fred</u><br/><u>Buckley</u>, <u>Marty Lewinter</u>.</li> <li>Introductory to Graph Theory, by <u>Fred Buckley</u>, <u>Marty</u><br/><u>Lewinter</u>.</li> </ol> |  |  |
| Supporting websites   | http://www.witno.com/philadelphia/courses.htm  |  |  |
| Teaching Environment  | ⊠Classroom □ laboratory ⊠Learning platform □Other  |  |  |

# Meetings and subjects timetable

| Week | Торіс  | Learning<br>Methods | Tasks | Learning<br>Material   |
|------|--|---------------------|-------|------------------------|
| 1    | Introduction to the uses of Graphs,<br>basic definitions, with special | Lecture             |       | Suggested<br>Questions |
| 1    | properties, Degree Sequence of a graph                                 |                     |       | for Practice           |

|       |   |         |                   | From<br>Lecture<br>Notes |
|-------|---|---------|-------------------|--------------------------|
|       |   |         |                   | Chapter # 1              |
| 2     | Isomorphism of graphs, subgraphs, self-<br>complementary graphs, connected<br>graphs and bridges.                     | Lecture | Assignment<br>#1  | Chapter # 1              |
| 3     | Adjacency matrix, permutation matrix, incidence matrix, degree matrix.  | Lecture |                   | Chapter # 1              |
| 4     | Trees and acyclic graphs, spanning trees, the matrix tree theorem.  | Lecture | Quiz 1            | Chapter # 2              |
| 5     | Weight matrix, Kruskal's and Prim's<br>algorithms for minimal spanning tree,<br>depth-first and breadth-first search. | Lecture |                   | Chapter # 2              |
| 6     | Walks in a graph, counting triangles subgraphs, distance and diameters.   | Lecture | Midterm<br>Exam   | Chapter # 3              |
| 7     | Distance matrix, distance in weighted graphs, Dijkstra's algorithm  | Lecture |                   | Chapter # 3              |
| 8     | Euler walk and Euler circuit, the Chinese postman problem   | Lecture |                   | Chapter # 3              |
| 9     | Hamilton cycles and Hamiltonian graphs, the traveling salesman problem and solutions for special cases.               | Lecture | Assignment<br># 2 | Chapter # 4              |
| 10    | Bipartite graphs and its coloring algorithm, complete and perfect matching, Hall's theorem.                           | Lecture |                   | Chapter # 4              |
| 11    | Chromatic number, sequential coloring<br>algorithm, Welsh-Powell coloring<br>algorithm.                               | Lecture |                   | Chapter # 4              |
| 12    | Planar graphs, proving planarity using<br>Hamilton cycles.  | Lecture | Quiz 2            | Chapter # 4              |
| 13    | Regions of a plane graph, Euler's<br>formula and planarity tests,<br>homeomorphism and Kuratowski's<br>theorem.       | Lecture |                   | Chapter # 4              |
| 14-15 | Maps and the dual graphs, the four-<br>color theorem and proofs of the six and<br>five-color theorems.                | Lecture |                   | Chapter # 4              |
| 16    | Final Exam  |         |                   |                          |

\* includes: Lecture, flipped Class, project- based learning, problem solving based learning, collaborative learning

#### **Course Contributing to Learner Skill Development**

Using Technology
Communication skills
Improve the communication skills of the student by giving oral quizzes and discuss the assignments
at the class

### **Assessment Methods and Grade Distribution**

| Assessment Methods    | Grade<br>Weight | Assessment Time<br>(Week No.) | Link to Course<br>Outcomes |
|-----------------------|-----------------|-------------------------------|----------------------------|
| Mid Term Exam         | 30%             | Week 6-8                      | K1,S1                      |
| Various Assessments * | 30%             | Continous                     | All of them                |
| Final Exam            | 40%             | Week 16                       | All of them                |
| Total                 | 100%            |                               |                            |

\* includes: quiz, in class and out of class assignment, presentations, reports, videotaped assignment, group or individual projects.

#### Alignment of Course Outcomes with Learning and Assessment Methods

| Number    | Learning Outcomes                              | Learning<br>Method* | Assessment<br>Method** |
|-----------|--|---------------------|------------------------|
|           | Knowledge                                      |                     |                        |
| K1        | Analyze the regularity of some graph.          | Lecture             | Exam,Assignment        |
|           | Determine whether or not a sequence is         |                     |                        |
|           | graphical. Determine the Isomorphism           |                     |                        |
|           | between two graphs. Produces a spanning        |                     |                        |
|           | tree of a graph. Produce a minimal spanning    |                     |                        |
|           | tree a graph. The concept of the isomorphism   |                     |                        |
|           | a weighted graph G.                            |                     |                        |
| K2        | Understand the concepts of Walk, Euler         | Lecture             | Exam, Quiz             |
|           | Walks, Cycles, Hamilton Cycles. Find the       |                     |                        |
|           | distance between the vertices. Find the        |                     |                        |
|           | shortest closed walk. Find the adjacency, and  |                     |                        |
|           | incidence matrices. Find the distance matrix.  |                     |                        |
| K3        | Coloring bipartite graphs. Determine when      | Lecture             | Exam, Quiz             |
|           | the graph is planar. Determine the Chromatic   |                     |                        |
|           | number. Understand the Regions of a plane      |                     |                        |
|           | graph. Know the Maps and the dual graphs.      |                     |                        |
|           | Skills   |                     |                        |
| <b>S1</b> | Understand mathematical definitions and        | Lecture             | Exam,Quiz              |
|           | demonstrate it in different graphs and writing |                     |                        |
|           | algorithms.                                    |                     |                        |
|           | Competencies                                   |                     |                        |
| C1        | Express thoughts in good logical writing       | Problem             | Assignment             |
|           | (Examples, Proofs,etc)                         | Solving             |                        |

\* includes: Lecture, flipped Class, project- based learning, problem solving based learning, collaborative learning

\*\* includes: quiz, in class and out of class assignment, presentations, reports, videotaped assignment, group or individual projects.

#### **Course Polices**

| Policy              | Policy Requirements  |  |  |  |  |
|---------------------|--|--|--|--|--|
| Passing Grade       | The minimum passing grade for the course is (50%) and the minimum final mark recorded on transcript is (35%).  |  |  |  |  |
| Missing Exams       | <ul> <li>Missing an exam without a valid excuse will result in a zero grade to be assigned to the exam or assessment.</li> <li>A Student who misses an exam or scheduled assessment, for a legitimate reason, must submit an official written excuse within a week from the exam or assessment due date.</li> </ul>  |  |  |  |  |
|                     | <ul> <li>A student who has an excuse for missing a final exam should submit the<br/>excuse to the dean within three days of the missed exam date.</li> </ul>   |  |  |  |  |
| Attendance          | The student is not allowed to be absent more than (15%) of the total hours prescribed for the course, which equates to six lectures days (M, W) and seven lectures (S,T,R). If the student misses more than (15%) of the total hours prescribed for the course without a satisfactory excuse accepted by the dean of the faculty, s/he will be prohibited from taking the final exam and the grade in that course is considered (zero), but if the absence is due to illness or a compulsive excuse accepted by the dean of the college, then withdrawal grade will be recorded. |  |  |  |  |
| Academic<br>Honesty | Philadelphia University pays special attention to the issue of academic integrity,<br>and the penalties stipulated in the university's instructions are applied to those<br>who are proven to have committed an act that violates academic integrity, such<br>as: cheating, plagiarism (academic theft), collusion, and violating intellectual<br>property rights.   |  |  |  |  |

# Program Learning Outcomes to be assessed in this Course

| Number | Learning Outcome  | Course<br>Title | Assessment<br>Method                          | Target<br>Performance<br>level |
|--------|---|-----------------|---|--------------------------------|
| Kp1    | Analyze the regularity of some graph.<br>Determine whether or not a sequence<br>is graphical. Determine the<br>Isomorphism between two graphs.<br>Produces a spanning tree of a graph.<br>Produce a minimal spanning tree a<br>graph. The concept of the<br>isomorphism a weighted graph G.   |                 | Lectures,<br>Assignments,<br>Exams,<br>Quizes |                                |
| Kp2    | Understand the concepts of Walk,<br>Euler Walks, Cycles, Hamilton Cycles.<br>Find the distance between the<br>vertices. Find the shortest closed<br>walk. Find the adjacency, and<br>incidence matrices. Find the distance<br>matrix. Coloring bipartite graphs.<br>Determine when the graph is planar.<br>Determine the Chromatic number.<br>Understand the Regions of a plane<br>graph. Know the Maps and the dual<br>graphs. |                 | Lectures,<br>Assignments,<br>Exams,<br>Quizes |                                |
| Sp1    | Understand mathematical definitions<br>and demonstrate it in different graphs<br>and writing algorithms.  |                 | Lectures,<br>Assignments,<br>Exams,<br>Quizes |                                |

| Cp1 | Express thoughts in good logical | Lectures,    |
|-----|----------------------------------|--------------|
|     | writing (Examples, Proofs,etc)   | Assignments, |
|     |                                  | Exams,       |
|     |                                  | Quizes       |

# Description of Program Learning Outcome Assessment Method

| Number | Detailed Description of Assessment           |
|--------|--|
| Kp1    | Short quizzes mainly (1) with 10 points each |
| Kp2    | Short quizzes mainly (3) with 10 points each |
| Sp1    | Quiz, Exam                                   |
| Cp1    | Assignment                                   |

# Assessment Rubric of the Program Learning Outcome